

"MINIMUM COST DIFFERENTIATION METHODS AND THEIR USES
IN UNDERSTANDING, DESIGNING AND OPTIMIZING COMPLEX SYSTEMS"

by Paul J. Werbos, Quality Assurance Division, 3/20/82

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